DESIGN OF FACTORIAL EXPERIMENTS IN SMALL BLOCKS

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ABSTRACT

The problem this study attempts to answer may be briefly described as follows. How can a factorial experiment be designed in a simple manner making use of whatever available blocks (which may or may not allow equal replication of treatments) so as to be able to estimate the important contrasts with a pre-specified order of precision?

The inverse variance covariance matrix Ω^{-1} for contrast effects (contrasts defined to be orthogonal to each other) obtained using least squares equations defines an important matrix which determines the block - contrast, and hence contrast - contrast non orthogonalities. This matrix is obtained by multiplying the matrix defining the set of contrasts w, and the incidence matrix of the design, n, and is termed the normalised basic score matrix, s. (s = w.n).

A zero basic score corresponding to a contrast and a block indicates that this contrast is orthogonal to the block. On the other hand, a higher (absolute) normalised basic score indicates a higher block - contrast non orthogonality.

The component $\underline{s}\underline{k}^{-\delta}\underline{s}$ of the diagonal element of $\underline{\Omega}^{-1}$ corresponding to a contrast defines the reduction of direct replication of a contrast due to blocking. This is termed 'the score for contrast e', and denoted by ss_e .

It appears that making ss_e small for a given contrast e ensures a higher precision for this contrast provided that the contrast is sufficiently replicated. However, this quantity can not be made small for all the contrast effects, since over a complete set of orthogonal contrasts, the sum of the contrast scores is a constant.

The procedure is simple and was found to be able to produce efficient small factorial designs. To assess its effectiveness in dealing with constructing large factorial designs the philosophy is translated in to a computer algorithm. Using this, it was found that the above method is capable of dealing with large factorials as well.

A brief study of constructing row and column designs using a similar principle is also included.