

## Automorphisms of Latin Squares

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A Latin Square  $L$  of order  $n$  is an  $n \times n$  array containing  $n$  symbols from  $[n] = \{1, 2, \dots, n\}$  such that each element of  $[n]$  appears once in each row and each column of  $L$ . Rows and columns of  $L$  are indexed by elements of  $[n]$ .

An automorphism  $\alpha$  of a Latin square is a permutation such that the triple  $(\alpha, \alpha, \alpha)$  maps the Latin square  $L$  to itself by permuting its rows, columns and symbols by  $\alpha$ . Let  $Aut(n)$  be the set of all automorphisms of Latin squares of order  $n$ . Whether a permutation  $\alpha$  belongs to  $Aut(n)$  depends only on the cycle structure of  $\alpha$ . Stones *et al.* [1] characterized  $\alpha \in Aut(n)$  for which  $\alpha$  has at most three non-trivial cycles (that is, cycles other than fixed points). A notable feature of this characterisation is that the length of the longest cycle of  $\alpha$  is always divisible by the length of every other cycle of  $\alpha$ . In this research we prove a related result for automorphisms with four non-trivial cycles.

**Keywords:** Latin Square, Automorphism, Cycle Structure, Permutation.

### References

1. Stones, D.S., Vojtěchovský, P. and Wanless, I.M., 2012. Cycle structure of autotopisms of quasigroups and Latin squares. *Journal of Combinatorial Designs*, 20(5), pp.227-263.